

# Representation of Collective Electrical Behavior of Cardiac Cell Sheets

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**ABSTRACT** The electrocardiogram (ECG) is a measure of the collective electrical behavior of the heart based on body surface measurements. With computational models or tissue preparations, various methods have been used to compute the pseudo-ECG (*p*ECG) of bipolar and unipolar leads that can be given clinical interpretation. When spatial maps of transmembrane potential ( $V_m$ ) are available, *p*ECG can be derived from a weighted sum of the spatial gradients of  $V_m$ . The concept of a lead field can be used to define sensitivity curves for different bipolar and unipolar leads and to determine an effective operating height for the bipolar lead position for a two-dimensional sheet of heart cells. The pseudo-vectorcardiogram (*p*VCG) is computed from orthogonal bipolar lead voltages, which are derived in this study from optical voltage maps of cultured monolayers of cardiac cells. Rate and propagation direction for paced activity, rotation frequency for reentrant activity, direction of the common pathway for figure-eight reentry, and transitions from paced activity to reentry can all be distinguished using the *p*VCG. In contrast, the unipolar *p*ECG does not clearly distinguish among many of the different types of electrical activity. We also show that *p*ECG can be rapidly computed by two geometrically weighted sums of  $V_m$ , one that is summed over the area of the cell sheet and the other over the perimeter of the cell sheet. Our results are compared with those of an ad hoc difference method used in the past that consists of a simple difference of the sum of transmembrane potentials on one side of a tissue sheet and that of the other.

## INTRODUCTION

The electrical activity of the heart produces electric potentials that can be measured at the body surface. Potential differences between points on the body surface provide the electrocardiogram (ECG), a time-dependent signal that encompasses the collective electrical behavior of the heart. The ECG is used clinically to distinguish among different conduction patterns such as sinus rhythm, tachycardia, and fibrillation (1). For in silico, in vitro, or ex vivo cardiac model systems, the pseudo-ECG (*p*ECG) provides a measure of the collective electrical behavior of the system. It has been applied to one- and two-dimensional computational models and two-dimensional slices or sheets of cardiac tissue. The value of the *p*ECG, as evidenced by its usage in the literature, is its representation of tissue-level effects as a clinical-like waveform even though the waveform contains less information than complete maps of  $V_m$ . In doing so, results obtained from simplified experimental systems can be interpreted and understood from a clinical perspective. Furthermore, like the ECG, the presence of beat-to-beat variations in activation and/or repolarization patterns at a global level become apparent.

Experimentally, *p*ECG has been measured in ex vivo preparations by bipolar electrodes placed on or around the tissue (2–4). However, when such recordings are unavailable or unfeasible to make, *p*ECG can be computed from spatial maps of transmembrane potential ( $V_m$ ). One approach that has been used is an ad hoc, difference method, which subtracts the average  $V_m$  from one-half of a myocardial tissue

layer from the average of the other half, as was done for thin ventricular epicardial slices and atrial tissue (5–8).

An alternative method used a theoretical approach to compute the extracellular potential at a particular point in space (i.e., for a unipolar lead), based on the model's spatial distribution of  $V_m$ , (9). A unipolar lead voltage was computed at a certain distance from the end of a one-dimensional multicellular fiber of coupled cardiac cells meant to represent the transmural heterogeneities in the ventricles. A unipolar lead has also been utilized in two-dimensional computation models (10,11).

In this study, we theoretically derive the bipolar and unipolar *p*ECGs for any desired lead location from optical recordings of  $V_m$  in a two-dimensional isotropic monolayer of cardiac cells. Further, we demonstrate that our expressions simplify to a weighted sum of  $V_m$ , scaled by two geometric functions. We then discuss the relative strengths and weaknesses of bipolar and unipolar *p*ECGs, through examples of different patterns of electrical propagation in cultured cardiac cell monolayers. We show that computation of the pseudo-vectorcardiogram (*p*VCG), based on an orthogonal pair of bipolar leads, clearly illustrates the collective electrical behavior of the cells and can be used to distinguish among different types of electrical activity.

## METHODS

### Theoretical considerations

#### *Bipolar pECG: ad hoc difference method*

A computationally simple *p*ECG can be obtained by subtracting the average of  $V_m$  from one-half of a cell sheet from that of the other half (6,12), which we

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refer to as the difference method. The pseudo-lead voltages along the  $x$  and  $y$  axes,  $pV_x^D$  and  $pV_y^D$ , are defined as

$$pV_x^D = \frac{\sum_{n, \text{right}} V_m}{n, \text{right}} - \frac{\sum_{n, \text{left}} V_m}{n, \text{left}}, \quad (1)$$

$$pV_y^D = \frac{\sum_{n, \text{top}} V_m}{n, \text{top}} - \frac{\sum_{n, \text{bottom}} V_m}{n, \text{bottom}}, \quad (2)$$

where  $n$  is the number of recorded sites in each half of the monolayer. The values  $pV_x^D$  and  $pV_y^D$  will be compared in the next section with the theoretically derived pseudo-lead voltages,  $pV_x$  and  $pV_y$ .

### Bipolar pECG: theoretical approach

We previously used the concept of a lead field to compute a bipolar pECG for cell monolayer experiments (13,14). Here, we generalize our approach and determine the pECG for any desired placement of lead electrodes. Let the cardiac cells occupy  $U$ , a circular two-dimensional area of radius  $R$  lying on the bottom of a semiinfinite bath. A bipolar lead is placed in the  $x$  direction, with electrodes at  $(a,0,h)$  and  $(-a,0,h)$ , respectively (Fig. 1, A and B). We define the pseudo-lead voltage,  $pV_x$ , as

$$\begin{aligned} pV_x &= \Phi_1 - \Phi_2 \\ &= \frac{1}{2\pi\sigma_b} \int_U \mathbf{J}^i \cdot \nabla \left( \frac{1}{r_1} \right) dx dy - \frac{1}{2\pi\sigma_b} \int_U \mathbf{J}^i \cdot \nabla \left( \frac{1}{r_2} \right) dx dy \\ &= \frac{1}{2\pi\sigma_b} \int_U \mathbf{J}^i \cdot \nabla \left( \frac{1}{r_1} - \frac{1}{r_2} \right) dx dy, \end{aligned} \quad (3)$$

where Eq. 3 is obtained as the superposition of dipole potentials (15).  $\mathbf{J}^i$  is the area density of bioelectric dipole current sources contained within  $U$ ,  $(1/2\pi\sigma_b)\nabla(1/r)$  is the dipole potential field,  $\sigma_b$  is the conductivity of the bath, and

$$r_1 = \sqrt{(x-a)^2 + y^2 + h^2}, \quad (4)$$

$$r_2 = \sqrt{(x+a)^2 + y^2 + h^2}. \quad (5)$$

$\mathbf{J}^i$  is the area density of the sum of dipole current sources directed along the  $x$  and  $y$  axes. Current sources that are directed along the  $x$  axis give rise to the  $x$  component of  $\mathbf{J}^i$ , and assuming that the cell sheet is isotropic with uniform intracellular surface conductivity  $g_i$  (equal to the intracellular conductivity  $\sigma_i$  times the sheet thickness),  $\mathbf{J}_x^i = -g_i(\partial\Phi_i/\partial x)\mathbf{a}_x$ , where  $\Phi_i$  is the intracellular potential, and  $\mathbf{a}_x$  is the unit vector in the  $x$  direction (15). A similar expression can be written for the  $y$  component of  $\mathbf{J}^i$ . Because  $V_m$  is equal to  $\Phi_i - \Phi_e$ , and because the cell monolayer lies in a conductive, semiinfinite bath (so that the extracellular potential  $\Phi_e$  is  $\ll \Phi_i$ ), gradients in  $\Phi_i$  are approximately equal to gradients in  $V_m$ . Accounting for the possibility that sources can be randomly oriented,

$$\mathbf{J}^i = -g_i \nabla V_m. \quad (6)$$

In the general case where intracellular conductivity is anisotropic,  $g_i$  would be replaced by an intracellular surface conductivity tensor. From Eq. 3 we can define a lead field,  $\mathbf{L}_{12}$ ,

$$\mathbf{L}_{12} = \nabla \left( \frac{1}{r_1} - \frac{1}{r_2} \right), \quad (7)$$

where  $\mathbf{L}_{12}$  is the sensitivity of the lead voltage to the sources  $\mathbf{J}^i$  located at different  $x,y$  positions. (Note that, from the reciprocity theorem,  $\mathbf{L}_{12}$  can be

interpreted as the electric field that would be produced in the  $x,y$  plane at point  $(x,y,0)$  for a unit current injected into the lead electrode at  $(-a,0,h)$  and withdrawn from the lead electrode at  $(a,0,h)$  (16).) Combining Eqs. 3 and 6,

$$pV_x = \kappa \int_U \nabla V_m \cdot \nabla \left( \frac{1}{r_2} - \frac{1}{r_1} \right) dx dy, \quad (8)$$

where

$$\kappa = \frac{g_i}{2\pi\sigma_b}. \quad (9)$$

Expanding the integrand, Eq. 8 becomes

$$pV_x = \kappa \int_U \left[ \left( \frac{x-a}{r_1^3} - \frac{x+a}{r_2^3} \right) \frac{\partial V_m}{\partial x} + \left( \frac{y}{r_1^3} - \frac{y}{r_2^3} \right) \frac{\partial V_m}{\partial y} \right] dx dy. \quad (10)$$

Experimentally,  $V_m$  was recorded at 253 discrete sites over a 17-mm-diameter area in confluent cell monolayers (17,18). The gradients are converted to differences in  $V_m$  interpolated between adjacent sites in the  $x,y$  plane, and the integral operation is replaced by a summation.

The method outlined above can be generalized to any placement of electrode leads. For example, a bipolar lead oriented in the  $y$  direction and situated a distance  $h$  above the monolayer, with electrodes a radial distance of  $a$  from the center, would have a pseudo-lead voltage of

$$pV_y = \kappa \int_U \left[ \left( \frac{x}{r_3^3} - \frac{x}{r_4^3} \right) \frac{\partial V_m}{\partial x} + \left( \frac{y-a}{r_3^3} - \frac{y+a}{r_4^3} \right) \frac{\partial V_m}{\partial y} \right] dx dy, \quad (11)$$

and  $r_3$  and  $r_4$  are defined as

$$r_3 = \sqrt{x^2 + (y-a)^2 + h^2}, \quad (12)$$

$$r_4 = \sqrt{x^2 + (y+a)^2 + h^2}. \quad (13)$$

An important factor to consider is the location of the lead electrodes. Assuming that they are symmetrically placed about the center of the monolayer, the two variables are the electrode displacement from the center of the monolayer,  $a$ , and the height above the monolayer,  $h$  (Fig. 1, A and B).  $\mathbf{L}_{12}$  (Eq. 7, Fig. 1 C) represents the sensitivity of the bipolar pECG to the negative transmembrane potential gradient at different locations in space. To quantify the lead sensitivity, the magnitude of  $\mathbf{L}_{12}$  along the primary (parallel to the axis of the lead) and secondary (perpendicular) axes was plotted with variation of  $h$  or  $a$ . Along both axes, the lead sensitivity decreases for increasing  $h$  (Fig. 1, D and E) as expected. Near the edge of the monolayer, directly below either of the lead electrodes, the sensitivity is at a minimum for all  $h$ . For small  $h$ , there is a near-edge region with heightened sensitivity along the primary axis, seen by the prominent side lobes in the sensitivity curve (Fig. 1 D). As  $h$  increases, both the sensitivity and the variation in sensitivity decrease over the monolayer. Ideally, the lead field is one that is as flat as possible. If we define the  $x$  axis as the primary axis, the lead sensitivity curve along the  $x$  axis as  $L_x = \mathbf{L}_{12} \cdot \mathbf{a}_x$ , and the effective operating height  $\bar{h}$  as the case where  $L_x$  is flat at the center of the monolayer (i.e.,  $d^2 L_x / dx^2$  at  $x=0$ ), then

$$\bar{h} = \frac{\sqrt{6}}{3} a. \quad (14)$$

The lead sensitivity curves at  $h = \bar{h}$  are shown as bold traces in Fig. 1, D and E, and are plotted in Fig. 1 F for increasing  $a$ . The width of the flat region can be defined to be that portion of the sensitivity curve along the primary axis that falls within 5% of the value in the center, in which case the width increases as  $h$  increases from 0 to just under  $\bar{h}$ , then decreases as  $h$  increases to a value of  $\sim \sqrt{2} \bar{h}$  and then increases again with further increases in  $h$  (not

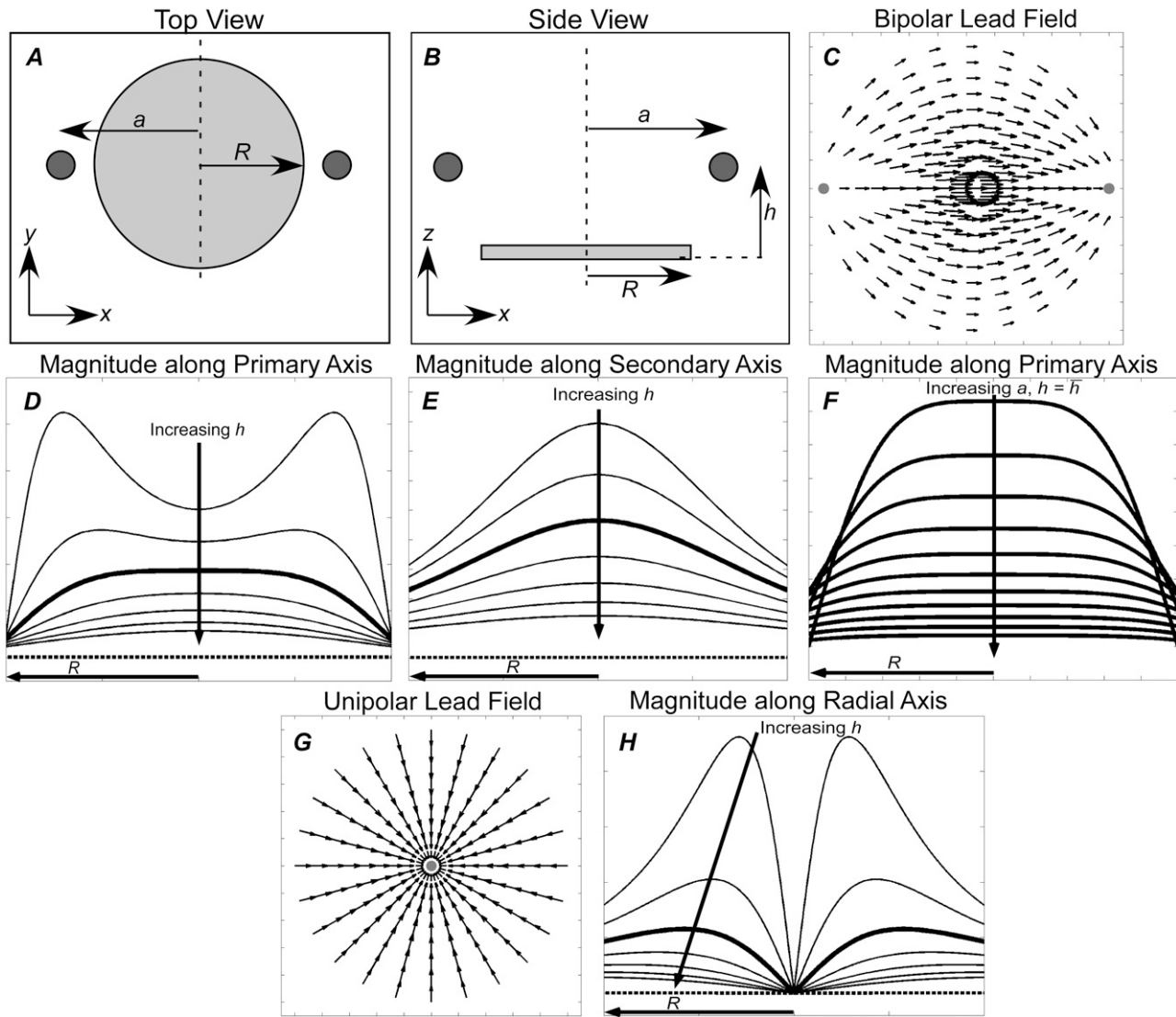


FIGURE 1 (A) Top view of monolayer and (B) side view of monolayer and bipolar lead electrode position. (C) Bipolar lead field, (D) lead field magnitude along primary axis ( $x$  axis in A), and (E) secondary axis ( $y$  axis in A) of bipolar lead field for increasing  $h$  (at  $a = R$ ). (F) Lead field magnitude along primary axis for increasing  $a$  at height  $\bar{h}$  ( $a \geq R$ ). (G) Unipolar lead field. (H) Lead field magnitude along radial axis of unipolar lead field for increasing  $h$  (at  $a = R$ ). For panels D–H,  $h$  is plotted from  $0.5\bar{h}$  to  $2\bar{h}$ , in steps of  $0.25\bar{h}$ , with  $h = \bar{h}$  shown as the bold trace. The case of  $h = 10\bar{h}$  is also plotted as the dashed trace. For panel F,  $a$  is plotted from  $R$  to  $2R$ , in steps of  $0.1R$ .

shown). Thus, measurement of the bipolar  $p$ ECG becomes a compromise between the magnitude and uniformity of the lead sensitivity with an effective operating height at  $h \approx \bar{h}$ . At  $h = \bar{h}$ , as  $a$  increases, the lead electrodes are farther from the monolayer and the width of the central region of uniform sensitivity increases, but sensitivity decreases (Fig. 1 F). For all bipolar  $p$ ECGs, we used the parameters  $a = R$  and  $h = \bar{h} \approx 0.82a$ , and in our experiments,  $a = 8.5$  mm. By comparison, in previous experimental studies we used the parameters  $a = R$  and  $h = 0.5a$  (13,14).

To facilitate their calculation,  $pV_x$  and  $pV_y$  can be expressed as integrals of  $V_m$  rather than integrals of derivatives of  $V_m$ . Green's first identity for the divergence theorem in two dimensions (for any two continuous functions,  $\phi$  and  $\psi$ ) is

$$\int_U (\nabla \phi \cdot \nabla \psi) dxdy = \oint_{\partial U} (\psi \nabla \phi \cdot \mathbf{n}) dl - \int_U (\psi \nabla^2 \phi) dxdy, \quad (15)$$

where  $\partial U$  is the boundary of  $U$ ,  $\mathbf{n}$  is the unit outer normal to the boundary, and  $dl$  is a differential element along the boundary. Setting  $\psi = V_m$  and  $\phi = \frac{1}{r_2} - \frac{1}{r_1}$ , and substituting Eq. 15 into Eq. 8,

$$pV_x = \kappa \oint_U V_m \nabla \left( \frac{1}{r_2} - \frac{1}{r_1} \right) \cdot \mathbf{n} dl - \kappa \int_U V_m \nabla^2 \left( \frac{1}{r_2} - \frac{1}{r_1} \right) dxdy. \quad (16)$$

Since  $U$  is a circular area with radius  $R$ , Eq. 16 simplifies to

$$pV_x = \oint_{\partial U} \alpha_x V_m dl + \int_U \gamma_x V_m dxdy, \quad (17)$$

where

$$\alpha_x = \frac{\kappa}{R} \left( x \left( \frac{x-a}{r_1^3} - \frac{x+a}{r_2^3} \right) + y \left( \frac{y}{r_1^3} - \frac{y}{r_2^3} \right) \right), \quad (18)$$

$$\begin{aligned} \gamma_x &= -\kappa \nabla^2 \left( \frac{1}{r_2} - \frac{1}{r_1} \right) \\ &= \kappa \left( \frac{3((x-a)^2 + y^2)}{r_1^5} - \frac{2}{r_1^3} - \frac{3((x+a)^2 + y^2)}{r_2^5} + \frac{2}{r_2^3} \right). \end{aligned} \quad (19)$$

Using a similar derivation, the voltage for a bipolar lead in the  $y$  direction for a circular cell monolayer with radius  $R$  is

$$pV_y = \oint_{\partial U} \alpha_y V_m dl + \int_U \gamma_y V_m dx dy, \quad (20)$$

where  $\alpha_y$  and  $\gamma_y$  are the geometric weighting functions,

$$\alpha_y = \frac{\kappa}{R} \left( x \left( \frac{x}{r_3^3} - \frac{x}{r_4^3} \right) + y \left( \frac{y-a}{r_3^3} - \frac{y+a}{r_4^3} \right) \right), \quad (21)$$

$$\gamma_y = \kappa \left( \frac{3((x^2 + (y-a)^2))}{r_3^5} - \frac{2}{r_3^3} - \frac{3((x^2 + (y+a)^2))}{r_4^5} + \frac{2}{r_4^3} \right). \quad (22)$$

The lead voltage is the sum of two terms: a boundary term (a weighted sum along the perimeter of the monolayer) and an area term (a weighted sum over the monolayer area). There can be significant differences in calculation times for the lead voltages, depending on the computational method used. Implementing Eq. 10 requires computation of a numerical gradient, which may necessitate signal processing such as spatial filtering or interpolation to reduce error. Implementing Eq. 17 does not require further processing, because the transmembrane potential values are used directly in the computation. For a two-second optical recording at 1-ms time resolution with 253 recording sites in our cell monolayers, using Eq. 10 requires interpolation of our hexagonal recording array and takes  $\sim 1$  min to compute, whereas using Eq. 17 takes  $< 1$  s to compute (on an Intel Pentium M 1.6 GHz processor). We confirmed the equivalency of Eqs. 10 and 17 for all of the examples presented in this study, and found negligible differences between the ensuing lead voltages except for some occasional minor baseline offsets that we attribute to discretization errors.

The ad hoc bipolar lead voltages ( $pV_x^D$  and  $pV_y^D$ ) are also integrals (sums) of  $V_m$  (see Eqs. 1 and 2) but have different weighting functions for  $V_m$  ( $\gamma_x^D$  and  $\gamma_y^D$ ) compared with  $\gamma_x$  and  $\gamma_y$ , and do not include a boundary term at the perimeter of the monolayer (first term of Eq. 17). The value  $\gamma_x^D$  is a two-dimensional sign function, positive on one-half of the cell sheet and negative on the other half (Fig. 2 A). It is a coarse approximation of  $\gamma_x$  (see Eq. 19) at  $h = \bar{h}$  (Fig. 2 C). The value  $\gamma_x$  is also shown at other values of  $h$  (normalized to the maximum of  $\gamma_x$  at  $h = \bar{h}$ ). It increases sharply near the electrodes at  $h = 0.5\bar{h}$  (Fig. 2 B) and becomes much flatter and linear in shape at  $h = 2\bar{h}$  (Fig. 2 D). At large  $h$  ( $h = 10\bar{h}$ ),  $\gamma_x$  approaches a flat plane tilted around the  $y$  axis (Fig. 2 E). The value  $\alpha_x$  has a maximum amplitude directly below the electrodes, at  $\theta = 0$  and  $\pi$ , and is zero in the  $y$  direction at  $\theta = \pi/2$  and  $-\pi/2$  (Fig. 2 F). At  $h = 0.5\bar{h}$  (Fig. 2 F, *dashed black trace*),  $\alpha_x$  has sharper peaks and a larger amplitude below the electrodes, compared with  $h = \bar{h}$  (Fig. 2 D, *solid black trace*). At  $h = 2\bar{h}$  (Fig. 2 F, *dashed shaded trace*),  $\alpha_x$  has a flatter angular dependence and a lower amplitude under the electrodes. At  $h = 10\bar{h}$  (Fig. 2 F, *solid shaded trace*),  $\alpha_x$  is near zero at all locations. The amplitude of  $\alpha_x$  has been scaled by the ratio of the monolayer circumference to area (and normalized to the maximum of  $\gamma_x$  at  $h = \bar{h}$ ) to allow comparison with  $\gamma_x$ . At  $h = \bar{h}$ , the maximum value of  $\alpha_x$  is  $< 10\%$  of  $\gamma_x$ . For increasing  $h$ , the amplitude of  $\gamma_x$  decreases at a faster rate than that of  $\alpha_x$  and therefore the relative weight of the boundary term increases.

## Pseudo-vectorcardiogram (pVCG)

The pseudo-vectorcardiogram (pVCG) is obtained by plotting  $pV_y$  against  $pV_x$ . For comparison, the pseudo-vectorcardiogram ( $pVCG^D$ ) is also obtained by plotting  $pV_x^D$  against  $pV_y^D$ .

## Unipolar pECG: theoretical approach

A unipolar (single electrode) lead, placed at  $(a, b, h)$  with reference at infinity, can be used for pECG measurements instead of the bipolar leads. The derivation of the unipolar lead voltage  $pV_0$  closely follows that of the bipolar lead voltage. The unipolar lead was placed over the center of the monolayer ( $a = 0, b = 0$ ) unless otherwise stated. The unipolar lead field,  $\mathbf{L}_0$ , is assumed to be for the case where the reference electrode is at infinity, and is given by

$$\mathbf{L}_0 = \nabla \left( \frac{1}{r_0} \right), \quad (23)$$

where

$$r_0 = \sqrt{(x-a)^2 + (y-b)^2 + h^2}. \quad (24)$$

$\mathbf{L}_0$  differs significantly from that of the bipolar lead. Instead of being primarily oriented along and sensitive to the  $x$  or  $y$  axis, the sensitivity of the unipolar lead is oriented radially outward from the electrode location (Fig. 1 G). The lead field is zero directly below the electrode, and therefore, the lead voltage is completely insensitive to electrical sources located there. The sensitivity rises sharply around the electrode location, becomes maximal at  $\rho = (\sqrt{2}/2)h$  (where  $\rho$  is the radial distance from  $(a, b, 0)$ ), and then drops off with increasing  $\rho$  (Fig. 1 H). As  $h$  increases, the overall lead sensitivity decreases, and the peak moves radially outward. For comparison with the bipolar lead,  $h$  was taken to be  $\bar{h}$ , for which the concavity of the sensitivity curve changes sign at the edge of the monolayer, at radius  $R$  (Fig. 1 H, *bold trace*).

The unipolar lead voltage,  $pV_0$ , is given by

$$pV_0 = -\kappa \int_U \nabla V_m \cdot \nabla \left( \frac{1}{r_0} \right) dx dy, \quad (25)$$

which can be expanded as

$$pV_0 = \kappa \int_U \left[ \left( \frac{x-a}{r_0^3} \right) \frac{\partial V_m}{\partial x} + \left( \frac{y-b}{r_0^3} \right) \frac{\partial V_m}{\partial y} \right] dx dy. \quad (26)$$

Alternatively, the lead voltage can be obtained as an integral of  $V_m$ ,

$$pV_0 = \oint_{\partial U} \alpha_0 V_m dl + \int_U \gamma_0 V_m dx dy, \quad (27)$$

where

$$\alpha_0 = \frac{\kappa}{R} \left( \frac{x(x-a) + y(y-b)}{r_0^3} \right), \quad (28)$$

$$\gamma_0 = \kappa \left( \frac{3((x-a)^2 + (y-b)^2)}{r_0^5} - \frac{2}{r_0^3} \right). \quad (29)$$

## Experimental methods

### Cell monolayer

Our cell culture procedure to create cell monolayers has been previously described (11,12). Briefly, neonatal rat ventricular myocytes were dissociated from two-day-old Sprague-Dawley rat hearts with the use of the enzymes, trypsin, and collagenase. The resulting cell suspension was plated at high density onto plastic coverslips to form monolayers that became confluent after

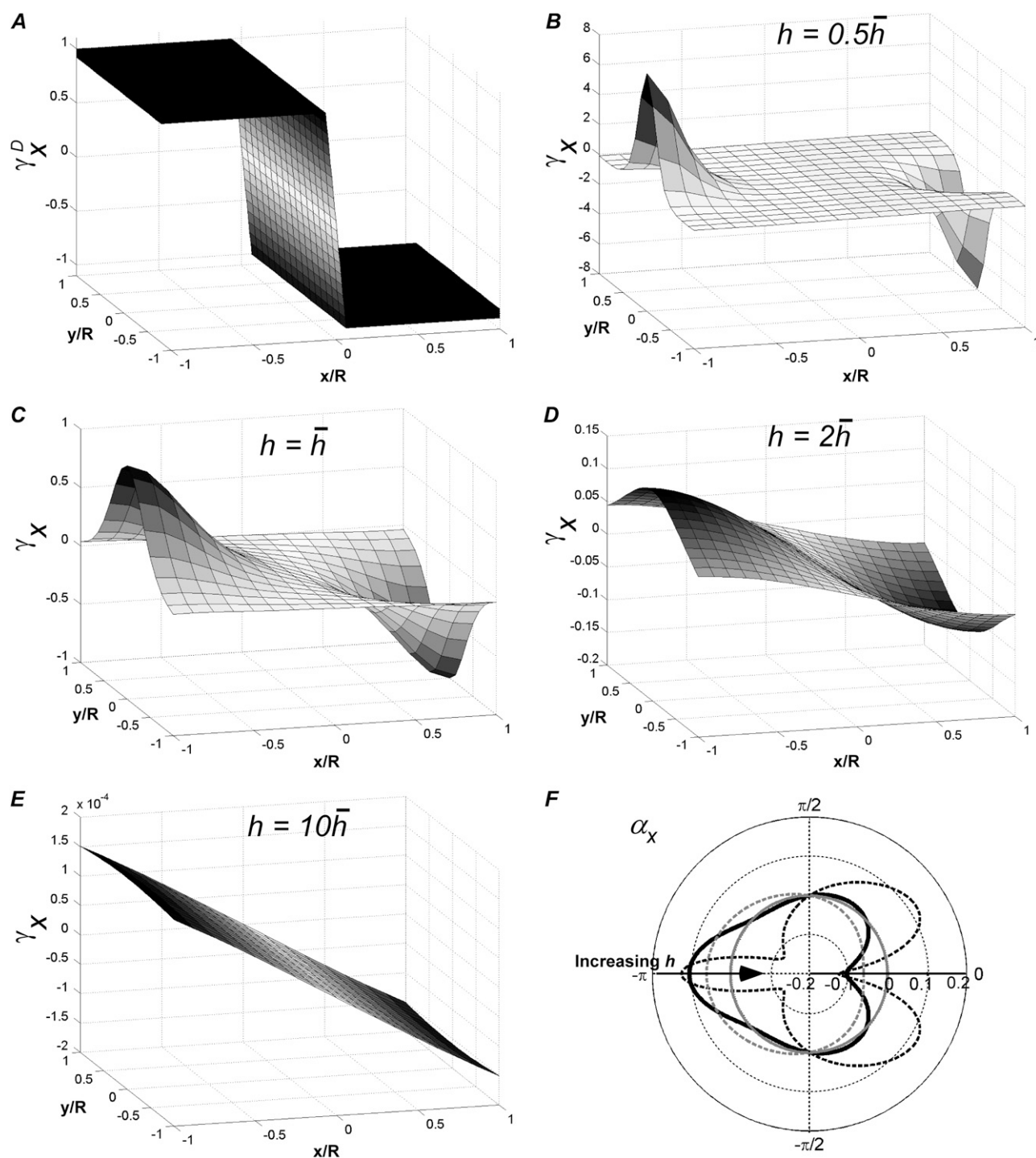


FIGURE 2 Weighting functions for bipolar pECGs. The value  $\gamma_x$ , computed by (A) difference method ( $\gamma_x^D$ ), and (B–E) theoretical method. For panels B–E,  $h = 0.5\bar{h}$ ,  $\bar{h}$ ,  $2\bar{h}$ , and  $10\bar{h}$ , respectively. (F) The value  $\alpha_x$ , computed by theoretical method is shown on a polar plot, with radial axis ranging from  $-0.2$  to  $0.2$ . For panel F,  $h = 0.5\bar{h}$  (dashed black trace),  $\bar{h}$  (solid black trace),  $2\bar{h}$  (dashed shaded trace), and  $10\bar{h}$  (shaded trace).

3–4 days of culture. Experiments were performed on days 4–9 after plating. The data for each example presented is from a different cell monolayer.

### Optical mapping

Our method of optical mapping of cell monolayers has been previously described (17,18). Briefly, maps of transmembrane potential were recorded

by placing the cell monolayer directly on top of a bundle of 253 optical fibers 1-mm in diameter, arranged in a tightly packed, 17-mm-diameter hexagonal array. During experiments, the cell monolayers were stained with  $10\ \mu\text{M}$  di-4-ANEPPS, a fluorescent voltage-sensitive dye, and continually superfused with warmed ( $36 \pm 0.5^\circ\text{C}$ ) oxygenated Tyrode's solution (in mmol/L: 135 NaCl, 5.4 KCl, 1.8  $\text{CaCl}_2$ , 1  $\text{MgCl}_2$ , 0.33  $\text{NaH}_2\text{PO}_4$ , 5 HEPES, 5 glucose). The fluorescent dye signal was relayed by the optical fiber bundle to an array

of photodetectors and amplifiers, processed by custom-written software and converted into pseudo-colored maps of  $V_m$ .

## Data analysis

To compare  $pVCG$ s calculated using the difference and theoretically derived methods, we first centered each  $pVCG$  at the origin by subtracting from  $V_x$  and  $V_y$  their respective mean values. We then determined the maximum excursion of the  $pVCG$  from the origin and normalized the radial distance of each  $pVCG$  point to that value. In this way, the  $pVCG$  lay within a unit circle. Using Eq. 30, we computed the root mean-square difference (RMSD) by taking the square root of the mean of the square of the difference (in percent) of the two traces at each time point,

$$RMSD = \sqrt{\frac{\sum_i^n [(pV_{x,i} - pV_{x,i}^D)^2 + (pV_{y,i} - pV_{y,i}^D)^2]}{n}}, \quad (30)$$

where  $i$  is the index of the data points at time  $t_i$  and  $n$  is the total number of time points.

## RESULTS

### Planar wave propagation

We show an example in Fig. 3 of a planar wave propagating across the monolayer that was initiated from a line electrode on the left side. The voltage map and isochrone map are shown in Fig. 3, A and B, respectively. The wave is propagating across

the monolayer primarily in the positive  $x$  direction, with a small component in the positive  $y$  direction. Both  $pV_x$  and  $pV_y$  are initially zero (Fig. 3 C a) and become positive (or negative) when the wavefront (or waveback) propagates across the monolayer.  $pV_x$  and  $pV_y$  are periodic at the pacing rate, larger during wavefront than waveback propagation (because of the larger transmembrane potential gradient), and approximately in phase with the same sign. It is possible for  $pV_x$  and  $pV_y$  to have opposite sign if the direction of propagation is toward the upper left or lower right (second or fourth quadrants) so that  $pV_x$  is negative while  $pV_y$  is positive, or vice versa.  $pVCG$  also reflects the direction of propagation and is oriented primarily in the  $x$  direction with a small component in the  $y$  direction (Fig. 3 D). The unipolar lead voltage  $pV_0$  (Fig. 3 C b) captures the general activity of planar wave propagation because there exists a component of the unipolar lead field (Fig. 1 H) that is oriented along the direction of propagation. However,  $pV_0$  does not indicate what the direction of propagation is, and it has a similar appearance for a wave propagating along any other direction across the monolayer.

### Radial wave propagation

We show a radial wave propagating outwardly from a point stimulus in Fig. 4 A. The position of the stimulus is slightly

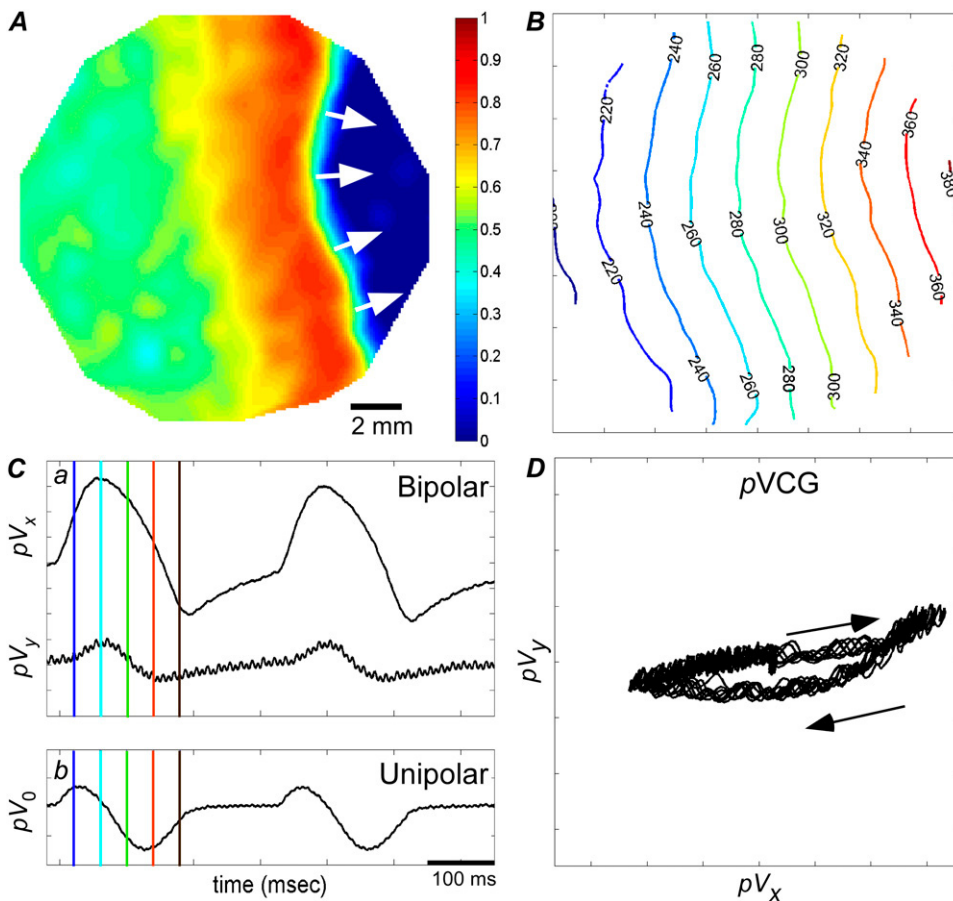


FIGURE 3 (A) Normalized voltage map for planar propagation. The color bar on the right indicates the relative amplitude of  $V_m$  (scaled from 0 to 1). (B) Isochrone map. (C) (a) Bipolar  $pVCG$ s ( $pV_x$  and  $pV_y$ ) and (b) unipolar  $pVCG$  ( $pV_0$ ). The colored vertical lines in panel C correspond to isochrones in the isochrone map in panel B. (D)  $pVCG$ . Arrows indicate the direction of  $pVCG$  with time.

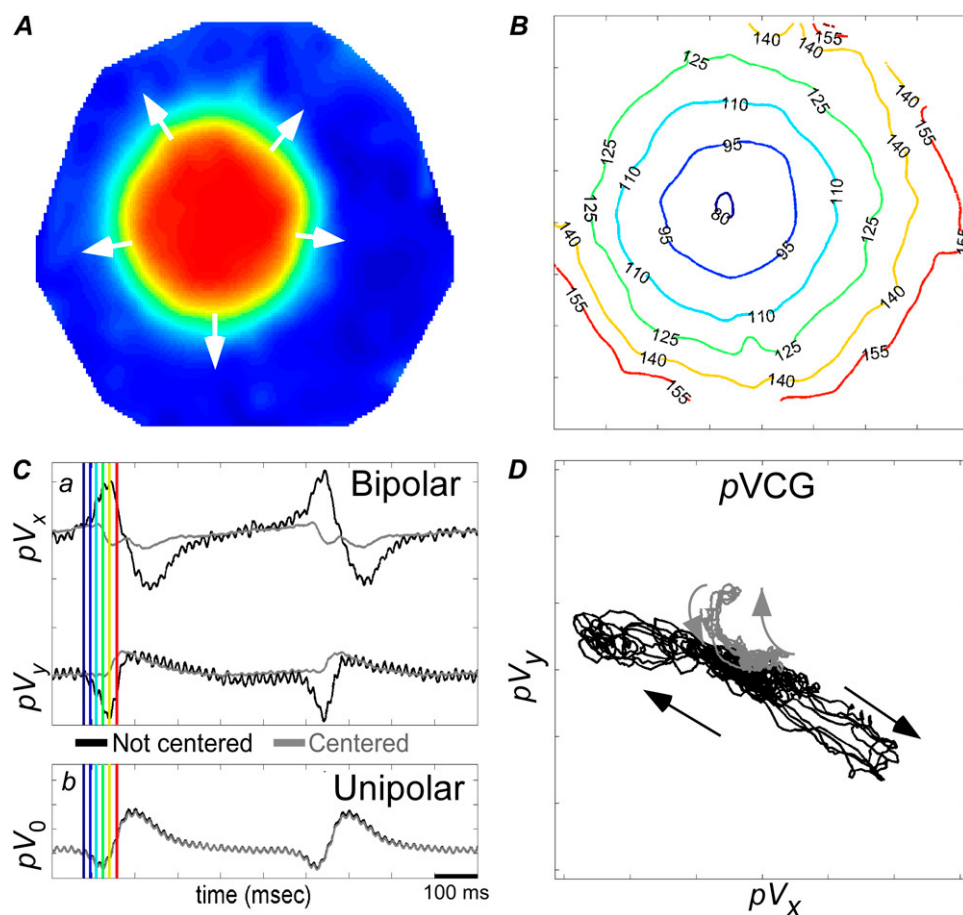


FIGURE 4 (A) Normalized voltage map for radial propagation. (B) Isochrone map. (C) (a) Bipolar  $pV_x$  and  $pV_y$  for leads placed asymmetrically around (solid traces) or centered on (shaded traces) the stimulus site, and (b) unipolar  $pECG$  ( $pV_0$ ) for lead offset from (solid trace) or centered on (shaded trace) the stimulus site. The shaded trace is covered by the solid trace at nearly all points and is difficult to see. (D)  $pVCG$  for bipolar leads placed asymmetrically (solid trace) or symmetrically (shaded trace) around the stimulus site. Different colors for the isochrones in panel B correspond to the instants of time shown in panel C.

off-center by  $\sim 1$  mm, toward the upper-left quadrant of the monolayer. Propagation terminates slightly sooner in the upper-left region, as seen in the isochrone map (Fig. 4 B). Because of the earlier termination of propagation in the upper-left region, residual propagation persists for a short time with an average direction toward the lower-right region. The  $x$  component (or  $y$  component) of the bipolar lead field is oriented in the same (or opposite) direction as the  $x$  (or  $y$ ) component of the residual wave. Therefore,  $pV_x$  (or  $pV_y$ ) shows positive (or negative) deflections during depolarization and negative (or positive) deflections during repolarization.  $pV_x$  and  $pV_y$  are approximately in phase with one another but have opposite signs (Fig. 4 C a, solid traces). The residual activity vector leads to large deflections in the  $pVCG$  in the lower right direction during depolarization and small deflections in the upper left direction during repolarization (Fig. 4 D, solid trace). To compute more balanced  $pECGs$  and  $pVCG$ , we can shift the lead placement so that the stimulus site is centered and then equalize the amount of tissue on all sides by taking an appropriate subset of optical recording sites. With this adjustment, the morphologies of  $pV_x$  and  $pV_y$  are altered (Fig. 4 C a, shaded traces), and  $pVCG$  remains close to the origin during wavefront propagation (Fig. 4 D, shaded trace). However, because the monolayer repolarizes nonuniformly in this example, the

waveback propagates more slowly in the lower-right direction. This results in a  $pVCG$  that retains a small deflection in the upper-left direction (Fig. 4 D, shaded trace).  $pV_0$  measured with the lead placed over the middle of the monolayer (Fig. 4 C b, solid trace) or centered over the stimulus site (Fig. 4 C b, shaded trace) measures the radial component of propagation, and the two are nearly identical. In the latter case, the unipolar lead field (Fig. 1 G) is completely aligned with the direction of propagation.

### Anchored spiral wave

In Fig. 5, a spiral wave is pinned to and propagating around a 3.5-mm-diameter hole near the center of the monolayer.  $pV_x$  and  $pV_y$  are periodic (at the rotation frequency of the spiral wave), sinusoidal, roughly equal in magnitude, and have an  $\sim 90^\circ$  phase difference (Fig. 5 C a, solid traces).  $pVCG$  is roughly circular (Fig. 5 D, solid trace), although with distinct bends because the hole is off-center and the amount of tissue differs on opposite sides of the hole. With a shift in the lead placement so that the hole is centered with equal amounts of tissue on all sides (like in the case of point stimulation),  $pV_x$  and  $pV_y$  are shifted slightly in time (Fig. 5 C a, shaded traces), and  $pVCG$  is more circular in shape (Fig. 5 D, shaded trace). Plotting  $pVCG$  in time (not shown) also reveals the direction



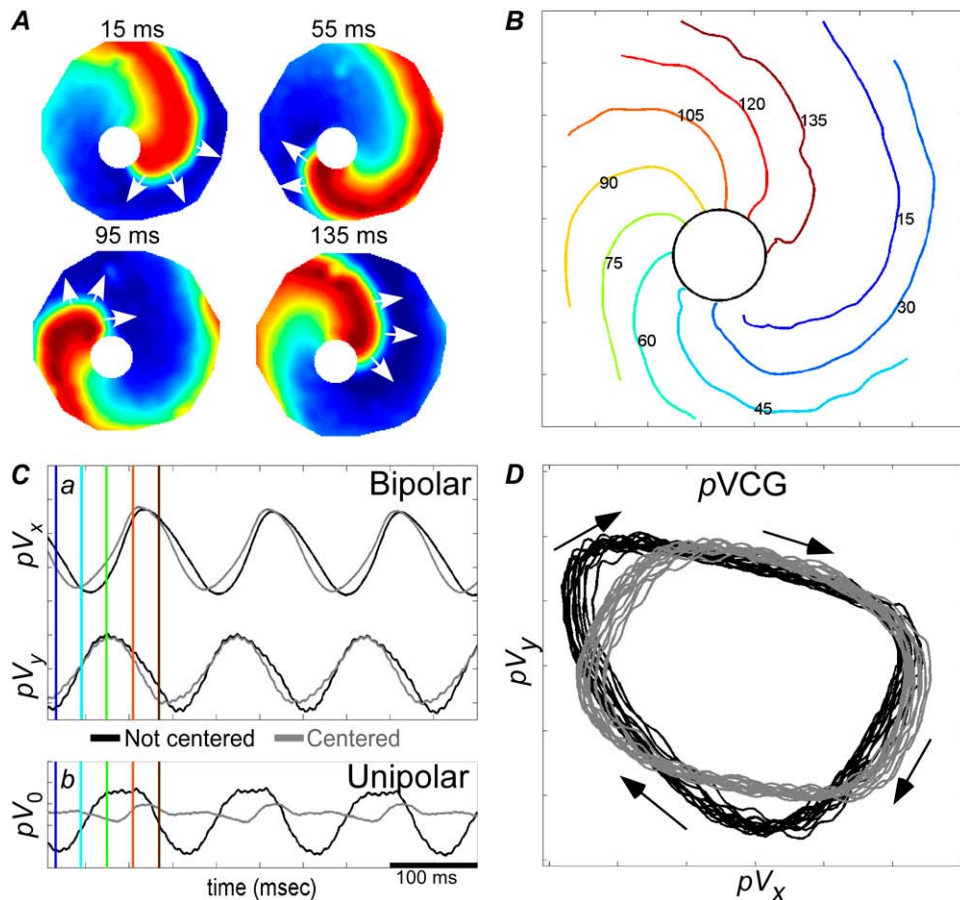


FIGURE 5 (A) Normalized voltage maps of spiral wave anchored to 3.5-mm-diameter hole. (B) Isochrone map. (C) (a) Bipolar  $pECGs$  ( $pV_x$  and  $pV_y$ ) for leads placed asymmetrically (solid traces) or symmetrically (shaded traces) around hole, and (b) unipolar  $pECG$  ( $pV_0$ ) for lead offset from (solid trace) or centered on (shaded trace) the hole. (D)  $pVCG$  for bipolar leads placed asymmetrically (solid trace) or symmetrically (shaded trace) around the hole. Different colors for the isochrones in panel B correspond to the instants of time shown in panel C.

of rotation (clockwise for this example). Slight variations in  $pV_x$  and  $pV_y$  amplitude and  $pVCG$  shape over successive cycles are due to small variations of the relative timing of the wavefront and waveback from cycle to cycle. With a unipolar lead placed directly above the center of the monolayer, a periodic waveform similar to albeit less sinusoidal than that obtained with the bipolar leads is observed (Fig. 5 C b, solid trace). Although the spiral wave moves primarily in a tangential direction perpendicular to the radially oriented unipolar lead field (Fig. 1 G),  $pV_0$  oscillates at the spiral wave period because of the offset position of the unipolar lead from the center of the hole, which renders components of the lead field to be more sensitive to the wave movement. However, if the lead position is shifted so that it lies over the center of the hole, the lead field is relatively insensitive to wavefront propagation.  $pV_0$  acquires a low-amplitude, harmonic component (Fig. 5 C b, shaded trace) at twice the reentry rate, which is a typical observation at the core of a spiral wave (6). Regardless of lead placement,  $pV_0$  does not contain information regarding the direction of rotation.

### Figure-eight reentry

A figure-eight reentry was initiated by rapid pacing followed by a premature stimulus. The reentry wave consists of a pair

of entrained spiral waves that rotate in opposite directions and merge during part of the cycle along a common pathway. In the example shown in Fig. 6 A, the axis of the common pathway (the open line delineating the collision site of the two spiral wave bands) happens to slowly rotate in the clockwise direction with successive cycles. The lead voltages are periodic at the rotation frequency of the reentry, and the phase difference between  $pV_x$  and  $pV_y$  varies during each cycle and from cycle to cycle (cycles shown with different colors, Fig. 6 B a).  $pVCG$  is elliptical in shape, with the primary axis parallel to the common pathway (Fig. 6 C). The primary axis of the ellipse rotates in the clockwise direction with successive cycles.  $pV_0$  is a noisy, irregular trace with varying frequency and amplitude, and information concerning the rotation frequency or common pathway of the reentry is absent (Fig. 6 B b).

### Transition 1: transition from paced propagation to spiral wave

In Fig. 7 A, point stimulation near the edge produces a wave propagating mostly in the positive  $y$  direction, with a small component in the negative  $x$  direction (0–60 ms). The wave moves through a heterogeneous region in the center of the monolayer, where conduction velocity is slower. The next



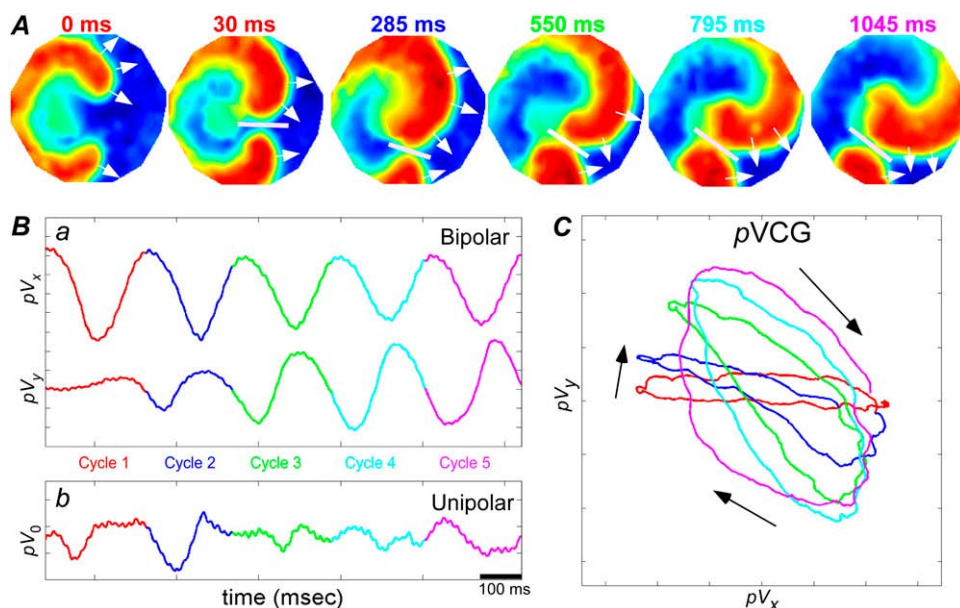


FIGURE 6 (A) Normalized voltage maps of rotating figure-eight reentry. (B) (a) Bipolar pECGs ( $pV_x$  and  $pV_y$ ) and (b) unipolar pECG ( $pV_0$ ). (C) pVCG. Different colors for the times in panel A correspond to different cycles and are the same as in panels B and C.

stimulated wave breaks (80–100 ms) and forms a spiral wave anchored to the heterogeneous region (120–210 ms).  $pV_x$  and  $pV_y$  have broad deflections during paced propagation and appear sinusoidal during spiral wave propagation (Fig. 7 B a).  $pVCG$  mirrors the direction of paced propagation— $pV_x$  is increasingly negative and  $pV_y$  is increasingly positive during

wavefront propagation, leading to a deflection in the upper-left direction.  $pV_x$ ,  $pV_y$ , and  $pVCG$  all demonstrate the transition from paced propagation to a spiral wave and is clearest for  $pVCG$  (Fig. 7 B a and C). The transition is also apparent in the phase difference between the two lead voltages, changing from  $\sim 0^\circ$  (with opposite sign) to  $\sim 90^\circ$ , as indicated by the de-

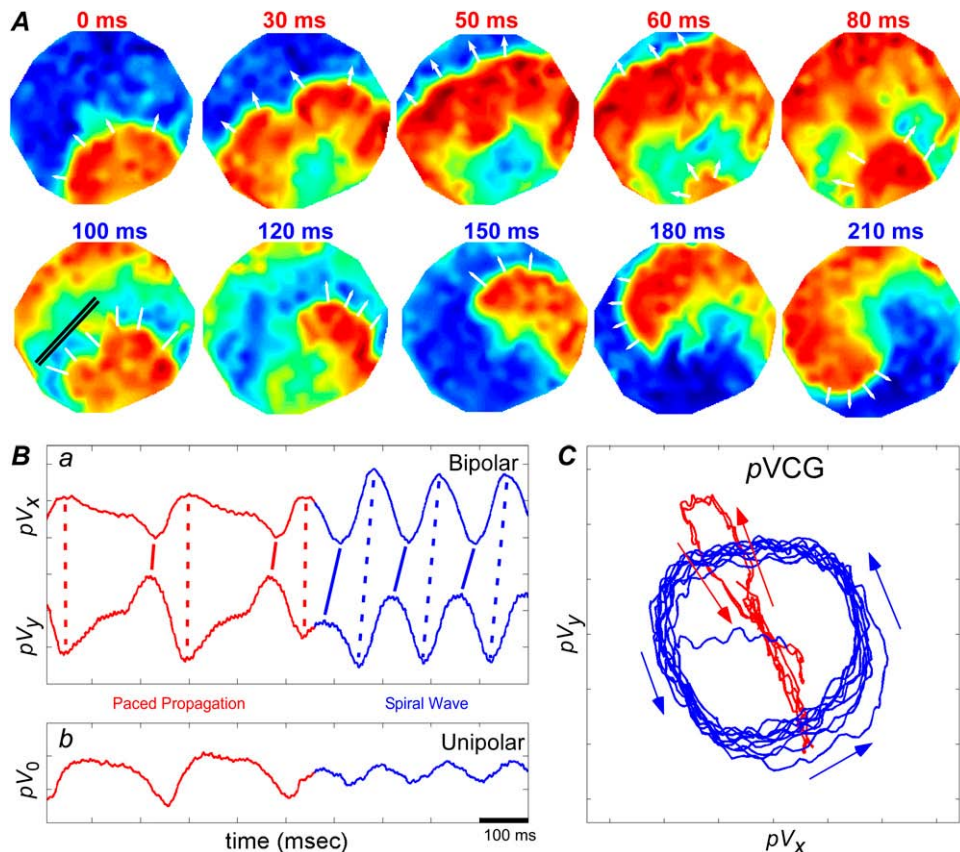


FIGURE 7 (A) Normalized voltage maps during transition from paced wave to spiral wave. (B) (a) Bipolar pECGs ( $pV_x$  and  $pV_y$ ) and (b) unipolar pECG ( $pV_0$ ). Vertical bars have been added to mark the relative timing of the peaks and valleys. (C) pVCG. Different colors in the times in panel A correspond to different propagation patterns and are the same as in panels B and C.

creased tilts of the vertical timing marks (compare *blue* versus corresponding *red* marks). Like  $pV_x$  and  $pV_y$ , the value  $pV_0$  shows a change in morphology upon the transition, with sharp deflections during paced propagation and a sinusoidal shape during the spiral wave (Fig. 7 B b).

### Transition 2: a complex transition

A more complex transition between electrical behaviors is illustrated in Fig. 8. As shown in Fig. 8 A, the monolayer was initially paced from a point stimulus electrode near the edge (0 ms). A heterogeneous region in the center of the monolayer caused wavebreak (20 ms), leading to a figure-eight reentry after pacing ended (60–235 ms). The figure-eight reentrant wave eventually transitioned into a single spiral wave rotating around the center region (705–955 ms). For clarification, the times are colored differently during the three propagation patterns. The bipolar lead voltages transition from single deflections to sinusoids, as behavior changes from paced propagation to reentry (Fig. 8 B). The lead voltages are in phase with opposite sign during paced propagation and are on average  $\sim 90^\circ$  out of phase during spiral wave propagation, as shown by the decreased tilts of the vertical timing marks. The phase difference varies during figure-eight

reentry. Both transitions are difficult to identify from a single lead voltage trace. However,  $pVCG$  differentiates the three behaviors clearly (Fig. 8 C). The initial pacing is illustrated by a fairly linear  $pVCG$  (*red* trace), which becomes elliptical for the figure-eight reentry (*blue* trace) and circular for the single spiral wave (*green* trace). Regarding  $pV_0$ , it is not clear from this signal alone what type of propagation is initially present, although some kind of transition is evident by the large jump in amplitude after  $\sim 600$  ms that is followed by a more sinusoidal shape. The transition from figure-eight reentry to single spiral wave also cannot be specifically identified, although some kind of transition is apparent by the appearance of a high frequency component during the last 700 ms of the trace (Fig. 8 B b).

### Bipolar lead vectorcardiogram—dependence on height parameter $h$

For comparison,  $pVCG$  was computed at other heights ( $h = 0.5\bar{h}$ ,  $2\bar{h}$ , and  $10\bar{h}$ ) for the six examples presented earlier.  $pVCG$ s at  $0.5\bar{h}$  (Fig. 9 A) are distorted from the  $pVCG$ s at  $\bar{h}$  (Fig. 9 B). For the planar wave,  $pVCG$  loses its linear shape. The spiral wave  $pVCG$  is less circular and has sharper corners. The figure-eight  $pVCG$  does not have a distinctly

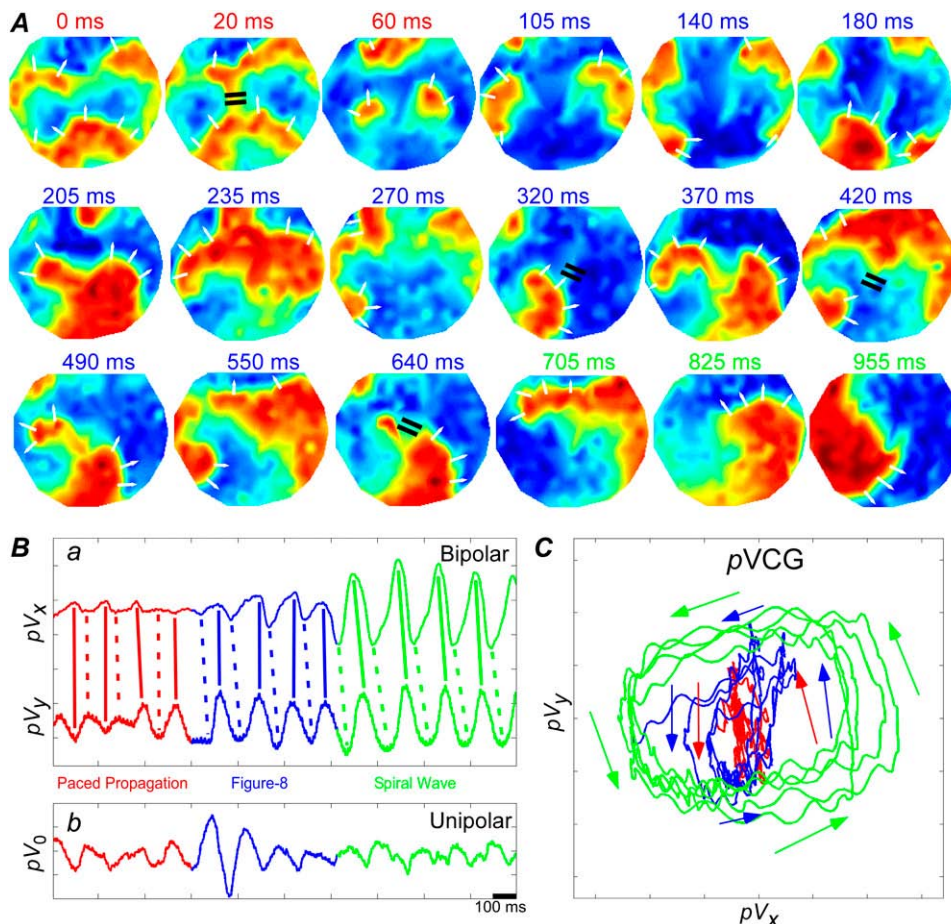


FIGURE 8 (A) Normalized voltage maps during transition from paced wave to figure-eight to spiral wave. (B) (a) Bipolar  $pECGs$  ( $pV_x$  and  $pV_y$ ) and (b) unipolar  $pECG$  ( $pV_0$ ). Vertical bars have been added to mark the relative timing of the peaks and valleys. (C)  $pVCG$ . Different colors in the times in panel A correspond to different propagation patterns and are the same as in panels B and C.



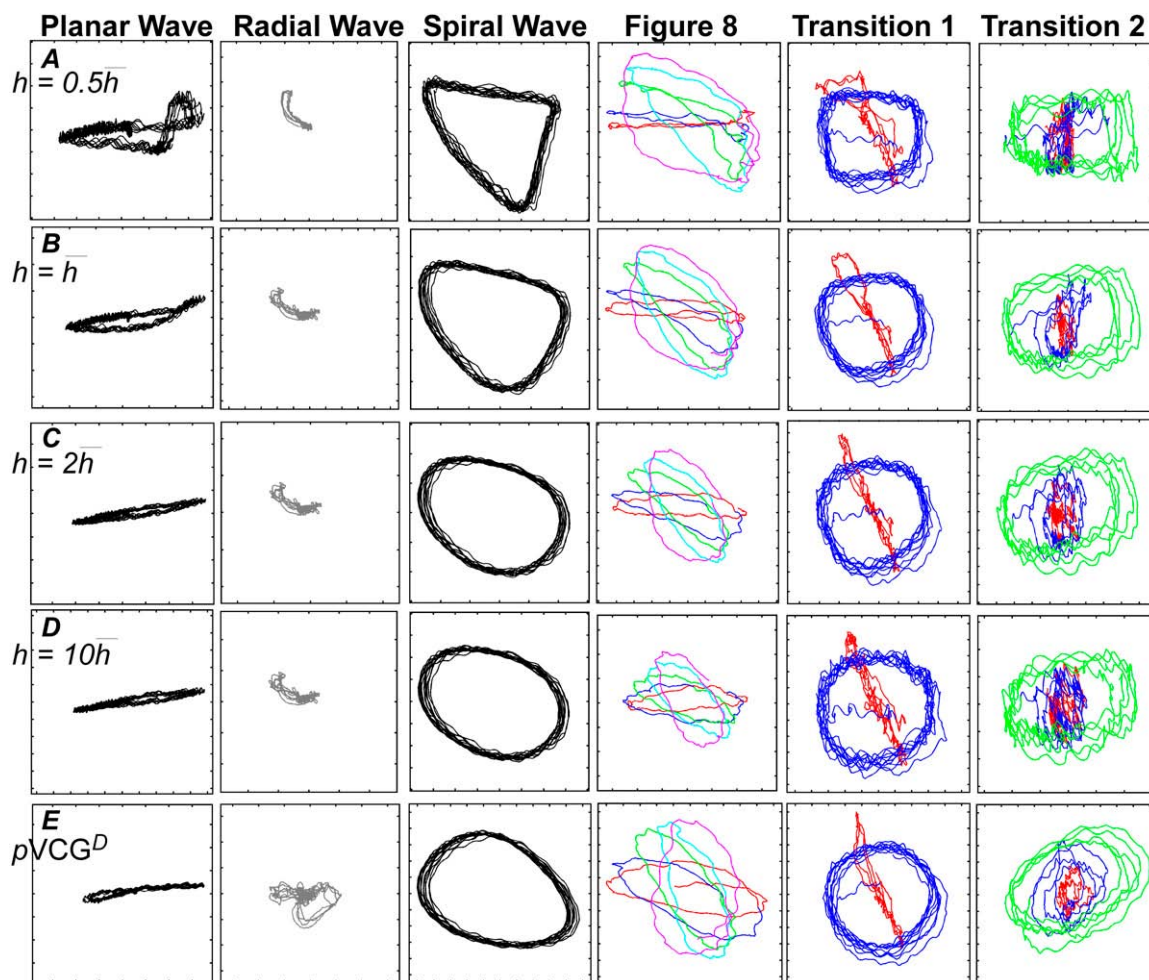


FIGURE 9  $pVCG$ s calculated at (A)  $h = 0.5\bar{h}$ , (B)  $h = \bar{h}$ , (C)  $h = 2\bar{h}$ , (D)  $h = 10\bar{h}$ , and  $pVCG^D$  (E) for six cases of wavefront propagation. The example for the radial wave has been centered. Each plot has been normalized to its own peak amplitude.  $pVCG$ s computed at  $h = 0.5\bar{h}$ ,  $h = \bar{h}$ ,  $h = 2\bar{h}$ , and  $h = 10\bar{h}$  have unnormalized relative amplitudes of  $\sim 2.5$ , 1, 0.3, and 0.0042, respectively.

elliptical shape. The transition from paced propagation to spiral wave reentry (Transition 1) is identifiable, since the  $pVCG$  shape remains very different for the two behaviors. However, both the linear and circular shaped regions are distorted from their shapes at  $h = \bar{h}$ . Finally, the transition from paced propagation to figure-eight reentry (Transition 2) is not discernible.  $pVCG$ s at  $2\bar{h}$  and  $10\bar{h}$  (Fig. 9, C and D) are similar in all cases to  $pVCG$ s at  $\bar{h}$ , although with lower amplitudes. Hence, we conclude that  $\bar{h}$  is an effective operating height for the bipolar lead that yields lead signals that represent the global electrical behavior of the cell sheet in a manner akin to those of remote bipolar leads, while at the same time maintaining the amplitude of the signals (Fig. 1).

### Comparison of $pVCG$ s using difference and theoretically derived methods

$pVCG^D$  values calculated using the difference method are shown in Fig. 9 E for the six examples presented earlier using

the theoretical approach. For the most part,  $pVCG^D$  is similar to  $pVCG$  at  $h = \bar{h}$ , with some notable differences. For the example of radial propagation,  $pVCG^D$  does not show the small deflection found in  $pVCG$  owing to nonuniform repolarization, and for the anchored spiral wave,  $pVCG^D$  is rotated relative to  $pVCG$ . For Transition 2,  $pVCG^D$  is not as linear as  $pVCG$  during paced propagation, is more circular during the figure-eight reentry, and does not have as distinct a transition between figure-eight and single spiral wave reentry. We computed the root mean-square difference between normalized  $pVCG$  at  $h = \bar{h}$  and normalized  $pVCG^D$ , and the average percent error was 10.5% for all examples, with the largest differences for the radial (19.6%) and spiral (12.4%) waves.

### DISCUSSION

Although not in prevalent use today (19), the VCG has been used clinically to provide morphological interpretation of the electrical phenomena of the heart and continues to have di-

agnostic advantages over the ECG in certain situations (20). The VCG was first constructed in the frontal plane, based on the Einthoven limb leads (21). Since then the VCG was expanded to three dimensions (22), and compound lead systems were proposed to generate a set of orthogonal, corrected leads that compensated for internal inhomogeneities in torso conductance and geometry (23–25). Lead field analysis of the commonly used VCG systems quantified the uniformity and sensitivity of the leads in each dimension (26). Although the two-dimensional sheet lying in a bath is much simpler compared with the whole heart lying in the torso, lead field analysis has not been applied in this context and can be used to determine the sensitivity of the recording leads for the pseudo-ECG to the underlying cellular transmembrane potentials.

In this article, we present a formulation of bipolar  $p$ ECG and  $p$ VCG measurements of a two-dimensional cardiac sheet (cell monolayer) and analyze their dependence on lead placement. Further, we determine a mathematical relation for an effective operating height for the bipolar lead placed over opposite edges of the cell monolayer. Lead placement at half the effective height provides a  $p$ VCG that overweights the contribution of cells near the lead electrodes (Fig. 1), whereas  $p$ VCGs for bipolar leads at twice or 10-times  $\bar{h}$  is similar to that at  $\bar{h}$  (Fig. 9) but with lower amplitude. Therefore,  $\bar{h}$  can serve as the operating height that balances global sensitivity and amplitude for  $p$ ECG and  $p$ VCG computation.

Numerically calculated bipolar and unipolar leads have been used previously to approximate the clinical ECG for one- and two-dimensional studies (9–11,13). The numerical bipolar leads are analogous to the Einthoven limb leads, which measure the global activity of the heart. The numerical unipolar lead is analogous to the precordial leads,  $V_1$ – $V_6$  of the 12-lead system, that are placed on the chest to detect localized activity in the region of the heart closest to the lead (27,28). We find that for the case of a unipolar lead situated above a cardiac cell sheet, the unipolar  $p$ ECG is most sensitive to activity near the electrode, but importantly, it is insensitive to activity at the point directly underneath the electrode (Fig. 1  $H$ ). This is because at that location, electrical propagation is perpendicular to the three-dimensional lead field. However, in the three-dimensional heart, electrical activity can propagate parallel to the lead field, and therefore, the precordial leads are most sensitive to activity directly underneath that is propagating toward (or away from) the electrode.

There is growing use of monolayers as an *in vitro* system for investigating cardiac electrical behavior (29,30), and optical maps of transmembrane potential have enabled the study of different patterns of electrical propagation, as well as transitions between them in the context of arrhythmia (31). Electrical recordings of the VCG would be a valuable adjunct to optical maps because of their succinct representation of the electrical behavior, but are technically very difficult to obtain, owing to the extremely small extracellular potentials generated by a monolayer of cells in a bath. If we consider a 17-mm-diameter cardiac monolayer with intracellular con-

ductivity  $\sigma_i = 2.5$  mS/cm (32), a monolayer thickness of 10  $\mu$ m (33), placed in a bath with conductivity  $\sigma_b = 20$  mS/cm (34), and assume an action potential amplitude of 100 mV (35), a maximum transmembrane voltage upstroke velocity,  $(dV_m/dt)_{\max}$ , of 125 V/s (36), and a conduction velocity of 25 cm/s (37), an ECG measurement would have a peak value of  $\sim 4$   $\mu$ V. Instead,  $p$ ECG (and  $p$ VCG) can be determined from the optical maps of  $V_m$  using the methodology described in this study. Further, Iravanian and Christini have recently shown that it is possible to process optical signals for real-time control capability (38). Since  $p$ ECG is a weighted sum of  $V_m$  values, it can also be computed in real-time.

For two-dimensional propagation in cardiac cell monolayers, we have shown that the bipolar  $p$ VCG capably represents electrical propagation associated with plane waves, radial waves, reentrant spiral waves, figure-eight spiral waves, and transitions between them. Transitions from normal pacing behavior to a reentrant wave, or from a reentrant wave to multiple waves, are crucial cardiac events related to arrhythmia, and their detection is important. Plane waves appear as linear trajectories, radial waves as trajectories localized to the origin, single spiral waves as circles, and figure-eight spiral waves as ellipses. Phase differences between the bipolar lead voltages can also help to identify propagation patterns. The phase difference is  $\sim 0^\circ$  during paced propagation,  $90^\circ$  during spiral wave propagation, and variable during figure-eight reentries. In contrast, the unipolar  $p$ ECG does not represent some of these electrical activities well nor the transition between them. Key information such as direction of propagation or frequency of reentry is missing or may be distorted.

Finally, with the advent of optical mapping of  $V_m$  from tissue surfaces, bipolar  $p$ ECGs (lead voltages  $pV_x^D$  and  $pV_y^D$ ) were calculated in previous studies by using an ad hoc method that subtracts the sum of  $V_m$  on one-half of the mapped area from the sum of the other half (5–8,12). However, we have shown that two sets of geometric functions are necessary to correctly sum  $V_m$  for circular cardiac cell monolayers (sheets)—one set ( $\gamma_x$  and  $\gamma_y$ ) that is applied over the area of the monolayer and the other set ( $\alpha_x$  and  $\alpha_y$ ) that is applied over the perimeter of the monolayer. Their usage produces bipolar lead voltages  $pV_x$  and  $pV_y$  that are biophysically based, and also fast to compute, compared with alternative calculations based on the gradients of  $V_m$ .

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